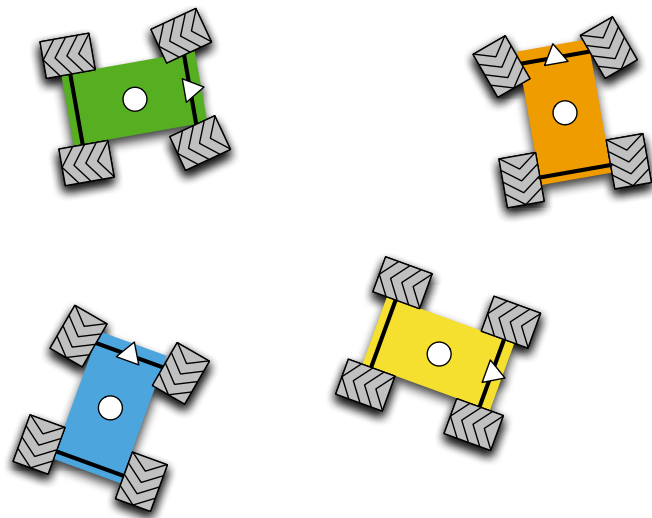# Distributed Control of Robotic Networks

A Mathematical Approach to Motion Coordination Algorithms

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